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Extending Three-Dimensional Weighted Cone Beam Filtered Backprojection (CB-FBP) Algorithm for Image Reconstruction in Volumetric CT at Low Helical Pitches

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A three-dimensional (3D) weighted helical cone beam filtered backprojection (CB-FBP) algorithm (namely, original 3D weighted helical CB-FBP algorithm) has already been proposed to reconstruct images from the projection data acquired along a helical trajectory in angular ranges up to \([0, 2\pi]\). However, an overscan is usually employed in the clinic to reconstruct tomographic images with superior noise characteristics at the most challenging anatomic structures, such as head and spine, extremity imaging, and CT angiography as well. To obtain the most achievable noise characteristics or dose efficiency in a helical overscan, we extended the 3D weighted helical CB-FBP algorithm to handle helical pitches that are smaller than 1 : 1 (namely extended 3D weighted helical CB-FBP algorithm). By decomposing a helical overscan with an angular range of \([0, 2\pi + \Delta \beta]\) into a union of full scans corresponding to an angular range of \([0, 2\pi]\), the extended 3D weighted function is a summation of all 3D weighting functions corresponding to each full scan. An experimental evaluation shows that the extended 3D weighted helical CB-FBP algorithm can improve noise characteristics or dose efficiency of the 3D weighted helical CB-FBP algorithm at a helical pitch smaller than 1 : 1, while its reconstruction accuracy and computational efficiency are maintained. It is believed that, such an efficient CB reconstruction algorithm that can provide superior noise characteristics or dose efficiency at low helical pitches may find its extensive applications in CT medical imaging.

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1. INTRODUCTION

Along with the fast evolution in theoretically exact helical cone beam (CB) reconstruction algorithms [1–5], in the recent years comes the exciting progress in theoretically approximate helical CB reconstruction algorithms [6–9]. A three-dimensional (3D) weighted helical CB filtered backprojection (CB-FBP) algorithm (namely, original 3D weighted helical CB-FBP algorithm) has been proposed to reconstruct images from the projection data acquired along a helical trajectory within an angular range up to \([0, 2\pi]\) [6]. Except for the adoption of 3D weighting functions, the original 3D weighted helical CB-FBP algorithm is essentially similar to the FDK algorithm [10] and its extensions [11]. By using phantoms simulated by computer and scanned by CB volumetric CT scanners, the reconstruction accuracy and other properties of the original 3D weighted helical CB-FBP algorithm have been experimentally evaluated and verified. Although it is theoretically approximate, the experimental evaluation shows that, at a moderate cone angle up to 4° that corresponds to a detector \(z\)-dimension of \(64 \times 0.625\) mm, the original 3D weighted helical CB-FBP algorithm reaches the reconstruction accuracy comparable to that of theoretically exact helical CB-FBP algorithms, such as the algorithm proposed by Katsevich [1, 2], and its extensions [3–5]. Moreover, other imaging performances, such as noise characteristics or dose efficiency, noise uniformity, spatial resolution, temporal resolution, computational efficiency, and robustness over clinical applications, are maintained comparable with the FDK-like CB reconstruction algorithms [10, 11].

A helical trajectory angular range of \([0, 2\pi]\) corresponds to a full scan [12, 13], under which the normalized helical pitch is usually about 1 : 1. However, a helical overscan is usually employed in the clinic to reconstruct tomographic images with superior noise characteristics at the most challenging anatomic structures, such as head and spine, extremity imaging, and CT angiography as well. In an overscan, the projection data acquired along a helical trajectory angular range larger than \([0, 2\pi]\) should be utilized to reconstruct an image, and the corresponding normalized
helical pitch is usually smaller than 1 : 1. Due to the $[0, 2\pi]$ constraint in helical trajectory angular range, a direct application of the original 3D weighted helical CB-FBP algorithm in an overscan cannot make full use of available projection data, resulting in a degraded noise characteristics or dose efficiency.

To improve noise characteristics or dose efficiency in an overscan, we extended the original 3D weighted helical CB-FBP algorithm to handle helical pitches that are lower than 1 : 1 (namely extended 3D weighted helical CB-FBP algorithm). As in the original algorithm, the extended algorithm can be implemented in either the native CB geometry or the cone-parallel geometry (or wedge-geometry) that is obtained through row-wise fan-to-parallel rebinning from the native CB geometry. An experimental study is conducted in this paper to evaluate the reconstruction accuracy and noise characteristics or dose efficiency of the extended 3D weighted helical CB-FBP algorithm. Since image reconstructed in the cone-parallel geometry is of better noise uniformity and computation efficiency, the experimental evaluation is carried out in the cone-parallel geometry using the helical body phantom (HBP) [14, 15] and the Defrise phantom [16] simulated by computer. As shown below, at helical overscan, the extended 3D weighted helical CB-FBP algorithm can provide significantly improved noise characteristics or dose efficiency in comparison to the original 3D weighted helical CB-FBP algorithm, while other advantages of the original algorithm, such as reconstruction accuracy and computational efficiency, can be maintained.

2. MATERIALS AND METHODS

2.1. Native cone beam and cone-parallel geometries

The native cone beam geometry for the helical projection data acquisition and image reconstruction is shown in Figure 1(a), where $Oxyz$ denotes the coordinate system, $S$ the source focal spot, $D$ the cylindrical multirow CT detector, and $R$ the radius of the helical source trajectory. $P(x, y, z)$ is a point within the object to be reconstructed. The ray emanating from focal spot $S$ and passing through point $P(x, y, z)$ is uniquely determined by its view angle $\beta$, fan angle $\gamma$, and cone angle $\alpha$. The helical source trajectory can be mathematically represented by

$$ST(\beta) = \left(R \sin \beta, R \cos \beta, \frac{H}{2\pi} \beta\right), \quad \beta \in [\beta_s, \beta_e],$$

where $\beta_s$ and $\beta_e$ are the starting and ending points of the helical source trajectory, respectively. Notice that view angle $\beta$ is defined in relative to the $y$-axis, and $H$ is the distance traveled by the source focal spot per rotation along the $z$-axis.

Through row-wise fan-to-parallel rebinning in the native CB geometry, the cone-parallel geometry for image reconstruction is attained as shown in Figure 1(b) [17–19]. The ray emanating from focal spot $S$ and passing through point $P(x, y, z)$ is uniquely determined by its view angle $\beta$, orthogonal distance $t$ from the iso-ray (namely orthogonal iso-distance), and cone angle $\alpha$.

![Figure 1: Schematic diagrams showing the geometries in which the extended 3D weighted helical CBFBP reconstruction algorithm is derived: (a) the native CB geometry; (b) the cone-parallel geometry.](image)

2.2. 3D weighted CB-FBP reconstruction algorithm

In the cone-parallel geometry shown in Figure 1(b), the original 3D weighted helical CB-FBP reconstruction algorithm for a full scan is [6]

$$\tilde{f}(x, y, z) = \frac{1}{2} \int_{\beta_n}^{\beta_{n+\pi}} \frac{R}{\sqrt{R^2 + Z^2(x, y, z)}} w_3d(\alpha, \beta, t)z(\alpha, \beta, t) d\beta,$$

$$z(\alpha, \beta, t) = s(\alpha, \beta, t) \otimes q(t),$$

where $Z(x, y, z)$ is the projected z-coordinate of point $P(x, y, z)$ onto detector $D$, and $q(t)$ is the conventional
ramp filter kernel in parallel beam geometry. The interval \([\beta_0 - \pi, \beta_0 + \pi]\) defines the view angle range over which the projection data are used to reconstruct an image intersecting the helical source trajectory at view angle \(\beta_0\). It is important to note that the filtering in (3) is naturally tangential [6, 20] due to the row-wise fan-to-parallel rebinning.

The 3D weighting function can be expressed in the form

\[
w_{3d}(\alpha, \beta, t) = \frac{w_{2d}(\beta, t) g(\alpha_c, p(h))}{w_{2d}(\beta, t) g(\alpha_c, p(h)) + w_{2d}(\beta_c, t) g(\alpha, p(h))},
\]

where \(\alpha\) and \(\alpha_c\) are the cone angles corresponding to a direct ray and its conjugate ray, respectively [6], and \(h\) is the normalized helical pitch defined by

\[
h = \frac{H}{L},
\]

where \(L\) represents the height of the detector along \(z\)-direction at the iso-center.

\(g(|\alpha|, p(h))\) is a monotonically increasing function over the magnitude of cone angle \(\alpha\), that is, given a normalized helical pitch \(h\), one has

\[
g(|\alpha_1|, p(h)) < g(|\alpha_2|, p(h)), \quad \text{while} \quad |\alpha_1| < |\alpha_2|,
\]

where \(p(h)\) is a monotonic increasing function of helical pitch \(h\), that is,

\[
p(h_1) < p(h_2), \quad \text{while} \quad h_1 < h_2,
\]

and the 3D weighting function \(w_{3d}(\alpha, \beta, \gamma)\) has to satisfy the normalization condition

\[
w_{3d}(\alpha, \beta, t) + w_{3d}(\alpha_c, \beta_c, t_c) = 1.0.
\]

Any 3D weighting function \(w_{3d}(\alpha, \beta, \gamma)\) satisfying the conditions specified by (6)–(8) is acceptable, and a special example is given by [6]

\[
w_{3d}(\alpha, \beta, \gamma) = \frac{w_{2d}(\beta, t) \tan k_h(\alpha_c)}{w_{2d}(\beta, t) \tan k_h(\alpha_c) + w_{2d}(\beta_c, t_c) \tan k_h(\alpha)},
\]

where \(k\) is a parameter that varies over different helical pitches, and can be adjusted to get a balanced capability between artifact suppression and noise characteristics. \(w_{2d}(\beta, t)\) is a 2D view weighting function and can find its examples in the literature [12, 13, 21–24].

### 2.3. Projection of reconstruction plane and 3D weighting

Prior to extending the original 3D weighted helical CB-FBP algorithm presented above, it is insightful for us to investigate the projection of reconstruction plane in helical scanning in the cone-parallel geometry. Supposing the reconstruction plane is orthogonal to the \(z\)-axis and intersects the helical source trajectory at \(\beta = 0^\circ\), shown in Figure 2(a) are the projections of reconstruction plane at helical pitch 63/64 : 1 corresponding to view angle \(\beta = -180^\circ, -90^\circ, -45^\circ, 0^\circ, 45^\circ, 90^\circ, 180^\circ\), respectively, in which the white area corresponds to the projection of the reconstruction plane, and the grey area the outside of the detector. At such a helical pitch, about half projection of the reconstruction plane at \(\beta = \pm 180^\circ\) is outside the detector boundary (detector \(z\)-dimension: \(64 \times 0.625\) mm), and this is the reason why 3D weighting is needed in the original 3D weighted helical CB-FBP algorithm to reconstruct images in a full scan [6]. However, at a lower helical pitch, such as 33/64 : 1 as shown in Figure 2(b), projections of the reconstruction plane at \(\beta = \pm 180^\circ\) are within the detector boundaries. Notice that, even at \(\beta = \pm 240^\circ\), a larger portion of the projection of reconstruction plane at pitch 33/64 : 1 is within the detector boundaries than that at helical pitch 63/64 : 1. Hence, it is intuitive to deduce that projection data corresponding to an overscan can be utilized at helical pitch 33/64 to reconstruct images with better noise characteristics or dose efficiency if the original 3D weighted helical CB-FBP algorithm can be extended to deal with overscan.
2.4. Extended 3D weighted helical CB-FBP algorithm

Suppose the angular range of projection data corresponding to an overscan is

\[ [\beta_{\text{min}}, \beta_{\text{max}}] = [0, 2\pi + \Delta\beta]. \] (10)

A direct extension of the original algorithm by just stretching the angular range from \([0, 2\pi]\) to \([0, 2\pi + \Delta\beta]\) violates the normalization condition specified in (8) and can result in artifacts in reconstructed images. However, if the helical trajectory angular range of an overscan \([0, 2\pi + \Delta\beta]\) is decomposed into a union of \(N\) overlapped subangular ranges

\[ [\beta_{\text{min,i}}, \beta_{\text{max,i}}] = \bigcup_{i=0}^{N-1} [\beta_{\text{min,i}}, \beta_{\text{max,i}}], \] (11)

and each subangular range spans \(2\pi\), that is,

\[ [\beta_{\text{min,i}}, \beta_{\text{max,i}}] = [0, 2\pi], \] (12)

the original 3D weighted helical CB-FBP algorithm can be extended to reconstruct images from projection data corresponding to an overscan in the way specified below:

\[
f(x, y, z) = \frac{1}{2N} \sum_{i=0}^{N-1} \frac{R}{\sqrt{R^2 + Z(x, y, z)^2}} w_{3d,i}(\alpha, \beta, t) s(\alpha, \beta, t) d\beta, \] (13)

where the support of each 3D weighting function \(w_{3d,i}(\alpha, \beta, t)\) is \([\beta_{\text{min,i}}, \beta_{\text{max,i}}]\), that is, view angle \(\beta_i\) has to be determined within each subangular range, respectively.

Since a filtered backprojection reconstruction algorithm is linear from the perspective of system analysis, (13) can be rearranged as

\[
f(x, y, z) = \frac{1}{2} \int_{\beta_{\text{min}}}^{\beta_{\text{max}}} \frac{R}{\sqrt{R^2 + Z(x, y, z)^2}} w_{3d}(\alpha, \beta, t) s(\alpha, \beta, t) d\beta, \] (14)

with

\[
w_{3d}(\alpha, \beta, t) = \frac{1}{N} \sum_{i=0}^{N-1} w_{3d,i}(\alpha, \beta, t), \] (15)

\[
w_{3d,i}(\alpha, \beta, \gamma) = \frac{w_{2d}(\beta, t) \tan^{kh}(\alpha_c)}{w_{2d}(\beta, t) \tan^{kh}(\alpha_c) + w_{2d}(\beta, t) \tan^{kh}(\alpha)}. \] (16)

This means that the reconstructed image under a helical overscan is just a linear summation of the images reconstructed from data acquired over a series of full scans corresponding to each subangular range \([\beta_{\text{min,i}}, \beta_{\text{max,i}}]\) \((\beta_{\text{max,i}} - \beta_{\text{min,i}} = 2\pi)\). The reconstruction accuracy corresponding to a full scan \([\beta_{\text{min,i}}, \beta_{\text{max,i}}]\) \((\beta_{\text{max,i}} - \beta_{\text{min,i}} = 2\pi)\) has been evaluated and verified in [6]. Consequently, the reconstruction accuracy of the extended 3D weighted helical CB-FBP algorithm specified by (13) or (14) is warranted as long as the overscan angular range \([\beta_{\text{min,o}}, \beta_{\text{max,o}}]\) \((\beta_{\text{max,o}} - \beta_{\text{min,o}} = 2\pi + \Delta\beta)\) is decomposed into subangular ranges appropriately. Note that \(N\) is a parameter that can be optimized under various low helical pitches to achieve a balance between the most achievable image quality and computational efficiency, and \(w_{2d}(\beta, t)\) can be in the form [12]

\[
w_{2d}(\beta, t) = \begin{cases} 0.0, & \beta \leq -\pi, \\ 0.25 \cdot \frac{(\beta + \pi)}{\beta}, & -\pi < \beta \leq -\pi + 2\beta, \\ 0.5, & -\pi + 2\beta < \beta \leq -2\beta, \\ 0.5 + 0.25(\beta + 2\beta), & -2\beta < \beta \leq 0, \\ 1.0 - 0.25\beta, & 0 < \beta \leq 2\beta, \\ 0.5, & 2\beta < \beta \leq \pi - 2\beta, \\ 0.5 - 0.25 \cdot \frac{(\beta - \pi + 2\beta)}{\beta}, & \pi - 2\beta < \beta \leq \pi, \\ 0.0, & \beta > \pi, \end{cases} \] (17)

where \(\beta_i\) is the parameter that can be adjusted to optimize the capability of suppressing artifacts and maintenance of noise characteristics or dose efficiency.

2.5. Evaluation

Just like the original algorithm, the extended 3D weighted helical CB-FBP algorithm is essentially approximate. Hence, the reconstruction accuracy of the extended algorithm has to be evaluated and verified experimentally. Two computer-simulated phantoms are utilized to evaluate the reconstruction accuracy. The first phantom is the helical body phantom (HBP) [14] to evaluate the reconstruction accuracy in transverse view, and the second is a modified Defrise phantom consisting of 5 cylindrical discs [15], rather than ellipsoidal discs in the original Defrise phantom, to evaluate the reconstruction accuracy in coronal view. The dimension of each disc is 200 \(\times\) 200 \(\times\) 10 mm\(^3\), centered at the z-axis, and their linear attenuation coefficient is equivalent to a CT number of 600 HU in reconstructed tomographic images. The central disc is located at \(z = 0\) mm, and other 4 discs are 20 mm apart along the z-direction. In the computer simulation, the distance from source to the iso-center of the volumetric CT is 541.0 mm, the X-ray detector consists of 64 detector rows and each detector row is made up of 888 detector cells with a dimension of 0.625 mm along z-axis and 0.5836 mm in xy-plane at the iso-center, respectively. The scanning techniques for the computer phantom simulation are 120 kVp, 300 mA, and 1.0 sec/rot, respectively. To quantitatively investigate noise characteristics or dose efficiency, a 20 cm water phantom scanned by a volumetric CT scanner (Lightspeed VCT, GE Healthcare, Waukesha, WI, USA) is employed. The matrix dimension of a reconstructed transverse image is 512 \(\times\) 512, no matter the projection data is...
simulated or scanned by the volumetric CT system, and 984 projections are simulated or scanned in one turn of the helical scanning (360°).

3. RESULTS

In general, the extended 3D weighted helical CB-FBP algorithm is applicable at any helical pitch lower than 1:1. Due to space limitation, only the results corresponding to helical pitch 33/64:1 and 63/64:1 are presented here. At helical pitch 33/64:1, the parameters of the weighting function are selected as \( \beta_t = 0.15\pi, \beta_{\text{max}} - \beta_{\text{min}} = 2.5\pi \), and \( N = 3 \), while the parameters of the weighting function are selected as \( \beta_t = 0.225\pi, \beta_{\text{max}} - \beta_{\text{min}} = 2.5\pi \) and \( N = 3 \), at helical pitch 63/64:1.

3.1. Evaluation of reconstruction accuracy

3.1.1. Evaluation by the HBP phantom

At helical pitch 33/64:1, the transverse image of the computer-simulated HBP phantom reconstructed by the extended algorithm using full-scan projection data is presented in Figure 3(a), while the one at the same location but reconstructed by the extended algorithm using overscan projection data is in Figure 3(b). The reconstruction field of view (FOV) is 450 mm, and no helical artifact is observed in both images, showing that the reconstruction accuracy of the extended algorithm is as good as that of the original algorithm. More specifically, it has to be revealed that \( kh = 0.25 \) for the original algorithm using full-scan projection data, while \( kh = 0.125 \) for the extended algorithm using overscan projection data to reconstruct the image.

At helical pitch 63/64:1, the transverse image of the HBP phantom reconstructed by the original algorithm using full-scan projection data is presented in Figure 3(c), while that at the same location but reconstructed by the extended algorithm using overscan projection data is in Figure 3(d). Again, no helical artifact is observed in both images, showing that the reconstruction accuracy of the extended algorithm is as good as that of the original algorithm at such a moderate helical pitch. Moreover, it has to be indicated that \( kh = 0.5 \) for both the extended and original algorithms using full-scan and overscan projection data, respectively.

3.1.2. Evaluation by the Defrise phantom

Multiple planar reformatted images in the coronal view of the Defrise phantom reconstructed by the original algorithm at helical pitch 33/64:1 using full-scan projection data is shown in Figure 4(a), while that by the extended algorithm using overscan projection data in Figure 4(b). Meanwhile, the coronal view of the Defrise phantom reconstructed by the original algorithm at helical pitch 63/64:1 using full-scan projection data is shown in Figure 4(c), while that by the extended algorithm using overscan projection data is in Figure 4(d). Just like the original reconstruction algorithm, the extended algorithm can reconstruct the Defrise phantom very well, showing that its reconstruction accuracy is comparable to the original 3D weighted helical CB-FBP algorithm.

3.2. Evaluation of noise characteristics or dose efficiency

A total of 5 ROIs are chosen within the 250 mm FOV of the 20 cm cylindrical water phantom to gauge the noise
in the 1st column of Table 1, and those corresponding to the extended algorithm are in the 2nd column. Apparently, the noise level at each ROI in the image reconstructed by the extended algorithm is significantly smaller than that in the image reconstructed by the original algorithm. Moreover, the noise uniformity at those ROIs in the image reconstructed by the extended algorithm is significantly better than that in the images reconstructed by the original algorithm. However, as shown in the right columns of Table 1, there is virtually no improvement in noise level and uniformity at helical pitch 63/64 : 1 in the images reconstructed by the extended algorithm over the original algorithm. This is consistent with our observation in Section 2.2, in which it has been shown that there is almost no extra projection data in comparison to a full scan can be utilized to reconstruct an image at helical pitch 63/64 : 1.

4. DISCUSSIONS AND CONCLUSIONS

It is well recognized that the 3D backprojection is the most computationally expensive process in image reconstruction using CB-FBP algorithms. It is important to point out that, the rearrangement of (13) into (14) not only simplifies algorithm expression but also improves image generation efficiency. In the implementation of (13), a total of $N$ images corresponding to projection data acquired along each sub-angular range and weighted by $w_{3d}(\alpha, \beta, t)$ have to be reconstructed using the original algorithm. However, in the implementation of (14), only one 3D backprojection is demanded to reconstruct image from projection data acquired along $[\beta_{\min,i}, \beta_{\max,i}]$ ($\beta_{\max,i} - \beta_{\min,i} = 2\pi$) and weighted by $w_{3d}(\alpha, \beta, t)$. Apparently, such an $N : 1$ ratio in computational complexity assures that the implementation of the extended 3D weighted helical CB-FBP algorithm by (14) is a better choice than that by (13) in practice.

It is worthwhile indicating that (11) and (12) do not demand each subangular range $[\beta_{\min,i}, \beta_{\max,i}]$ ($\beta_{\max,i} - \beta_{\min,i} = 2\pi$) evenly shifting in the decomposition to cover the whole angular range $[0, 2\pi + \Delta\beta]$, while an even shifting can result in data manipulation efficiency. Moreover, it is not mandatory for the 3D weighting function $w_{3d}(\alpha, \beta, t)$ corresponding to $[\beta_{\min,i}, \beta_{\max,i}]$ ($\beta_{\max,i} - \beta_{\min,i} = 2\pi + \Delta\beta$) to be the average of each 3D weighting function $w_{3d,j}(\alpha, \beta, t)$ corresponding to $[\beta_{\min,j}, \beta_{\max,j}]$ ($\beta_{\max,j} - \beta_{\min,j} = 2\pi$) as specified by (15). Indeed, other weighted summation strategies can be exercised in practice.

<table>
<thead>
<tr>
<th>ROI</th>
<th>Pitch = 33/64 : 1</th>
<th>Pitch = 63/64 : 1</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Full scan (kh = 0.125)</td>
<td>Overscan (kh = 0.125)</td>
</tr>
<tr>
<td>A</td>
<td>7.98</td>
<td>7.42</td>
</tr>
<tr>
<td>B</td>
<td>7.89</td>
<td>7.31</td>
</tr>
<tr>
<td>C</td>
<td>7.51</td>
<td>7.28</td>
</tr>
<tr>
<td>D</td>
<td>7.14</td>
<td>6.74</td>
</tr>
<tr>
<td>E</td>
<td>8.89</td>
<td>8.58</td>
</tr>
</tbody>
</table>
As indicated in [6], the original 3D weighted helical CB-FBP algorithm can be implemented in the native CB geometry, although its derivation in the cone-parallel geometry was given as an example in [6]. Hence, the extended 3D weighted helical CB-FBP algorithm can also be implemented in the native CB geometry as its counterpart. Moreover, it has to be pointed out that the determination of the parameters $\Delta \beta$ and $kh$ is not optimized in the experimental evaluation shown above. All the parameters chosen are just to show how the extended 3D weighted helical CB-FBP algorithm works in overscan corresponding to helical pitches lower than 1 : 1.

It has to be emphasized that both the original 3D weighting scheme proposed in [6] and the extended 3D weighting scheme presented in this manuscript are ray-wise weightings. This means that, by making use of the cone angle corresponding to both direct and conjugate rays, the 3D weighting is actually a ray-wise optimization process to obtain balanced image quality and most achievable dose efficiency over helical pitches. By making use of the cone angle information corresponding to conjugate rays, our ray-wise 3D weighting scheme distinguishes itself from other 3D weighting schemes existing in the literature [7–9]. The readers that are interested in the difference between our ray-wise 3D weighting scheme and that proposed in [7] are referred to [6], where a brief discussion on the difference is given. Detector-row-dependent weighting schemes have been proposed in [8, 9], respectively. By using predefined weighting distribution, the ray intercepting inner detector rows are given favorable weights and those intercepting outer detector rows are given unfavorable weights, in which the cone angle information corresponding to conjugate ray is not utilized. The weight in our method is ray-wise calculated and such a ray-wise optimization process can make use of redundant projection data as much as possible over helical pitches, particularly at high helical pitches. However, it seems very hard, if not impossible, to make use of projection data as much as possible by using a predefined weighting distribution in the detector as done in [8, 9]. Interested readers are referred to references [8, 9] for more detail.

Moreover, it should be indicated that the extended 3D weighted helical CB-FBP algorithm proposed in this manuscript is quite different from the n-PI CB reconstruction methods existing in the literature [25–27]. The concepts of Tam-window, PI-line, N-PI window, and N-PI line play critical roles in the derivation of both exact and approximate n-PI CB reconstruction algorithms. However, as clearly shown above, none of these concepts has been utilized in deriving the extended 3D weighted helical CB-FBP algorithm.

In summary, recognizing the clinical importance of reconstructing tomographic images from overscan projection data, the original 3D weighted helical CB-FBP algorithm has been extended in this manuscript to reconstruct tomographic images at helical pitches lower than 1 : 1. As shown in previous sections, such an extension can make use of projection data as efficient as possible, resulting in significantly improved noise characteristics or dose efficiency. In principle, the extended 3D weighted helical CB-FBP algorithm is approximate, but its reconstruction accuracy has been evaluated and verified at a relatively moderate cone angle ($4^\circ$) corresponding to a detector with the dimension of $64 \times 0.625$ mm at the source to iso-center distance of $541.0$ mm. In fact, the extended algorithm is expected to be applicable in volumetric CT scanners with the detector $z$-dimension corresponding to larger cone angles, and more investigation is being carried out to assure the maximum cone angle up to which the proposed algorithm can still provide acceptable reconstruction accuracy for diagnostic CT imaging applications.

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REFERENCES


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